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Relational Stacked Denoising Autoencoder for Tag Recommendation

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Abstract
Tag recommendation has become one of the most important ways of organizing and indexing online resources like articles, movies, and music. Since tagging information is usually very sparse, effective learning of the content representation for these resources is crucial to accurate tag recommendation. Recently, models proposed for tag recommendation, such as collaborative topic regression and its variants, have demonstrated promising accuracy. However, a limitation of these models is that, by using topic models like latent Dirichlet allocation as the key component, the learned representation may not be compact and effective enough. Moreover, since relational data exist as an auxiliary data source in many applications, it is desirable to incorporate such data into tag recommendation models. In this paper, we start with a deep learning model called stacked denoising autoencoder (SDAE) in an attempt to learn more effective content representation. We propose a probabilistic formulation for SDAE and then extend it to a relational SDAE (RSDAE) model. RSDAE jointly performs deep representation learning and relational learning in a principled way under a probabilistic framework. Experiments conducted on three real datasets show that both learning more effective representation and learning from relational data are beneficial steps to take to advance the state of the art.

Introduction
Due to the abundance of online resources like articles, movies, and music, tagging systems (Yu et al. 2014) have become increasingly important for organizing and indexing them. For example, CiteULike\(^1\) uses tags to help categorize millions of articles online and Flickr\(^2\) allows users to use tags to organize their photos. However, it is often not easy to compose a set of words appropriate for the resources. Besides, the large variety in phrasing styles of the users can potentially make the tagging information inconsistent and idiosyncratic. With such technical challenges, research in tag recommendation (TR) (Gupta et al. 2010; Wang et al. 2012) has gained in popularity over the past few years. An accurate tag recommendation system not only can save the pain of users searching for candidate tags on the tip of their tongues, but can also make the tags used more consistent. Consequently, both the user experience and recommendation accuracy can be improved dramatically.

Tag recommendation methods can roughly be categorized into three classes (Wang et al. 2012): content-based methods, co-occurrence based methods, and hybrid methods. Content-based methods (Chen et al. 2008; 2010; Shen and Fan 2010) utilize only the content information (e.g., abstracts of articles, image pixels, and music content) for tag recommendation. Co-occurrence based methods (Garg and Weber 2008; Weinberger, Slaney, and van Zwol 2008; Rendle and Schmidt-Thieme 2010) are similar to collaborative filtering (CF) methods (Li and Yeung 2011). The co-occurrence of tags among items, usually represented as an tag-item matrix, is used for tagging. The third class of methods (Wu et al. 2009; Wang and Blei 2011; Yang, Zhang, and Wang 2013; Zhao et al. 2013; Bao, Fang, and Zhang 2014; Chen et al. 2014), also the most popular and effective ones, consists of hybrid methods. They make use of both tagging (co-occurrence) information (the tag-item matrix) and item content information for recommendation.

In hybrid methods, learning of item representations (also called item latent factors in some models) is crucial for the recommendation accuracy especially when the tag-item matrix is extremely sparse. Recently, models like collaborative topic regression (CTR) (Wang and Blei 2011) and its variants (Purushotham, Liu, and Kuo 2012; Wang, Chen, and Li 2013) have been proposed and adapted for tag recommendation to achieve promising performance. These models use latent Dirichlet allocation (LDA) (Blei, Ng, and Jordan 2003) as the key component for learning item representations and use probabilistic matrix factorization (PMF) (Salakhutdinov and Mnih 2007) to process the co-occurrence matrix (tag-item matrix). However, when using LDA, the resulting item representations tend to be quite sparse. Consequently, more dimensions may be needed for the representations to be effective. Unfortunately PMF with the low-rank assumption usually works with quite a small number of latent dimensions, which is not in line with the nature of LDA (or CTR). On the other hand, deep learning models like stacked denoising autoencoder (SDAE) (Vincent et
al. 2010) and convolutional neural networks (Krizhevsky, Sutskever, and Hinton 2012) recently show great potential for learning effective and compact representations and deliver state-of-the-art performance in computer vision (Wang and Yeung 2013) and natural language processing (Salakhutdinov and Hinton 2009; Kalchbrenner, Grefenstette, and Blunsom 2014) applications. Intuitively, the effectiveness and compactness of deep learning models like SDAE seem to fit PMF perfectly and can potentially lead to significant boost of recommendation performance. Besides, since relational data exist as an auxiliary data source in many applications (e.g., natural language processing, computational biology), it is desirable to incorporate such data into tag recommendation models. For example, when recommending tags for articles in CiteULike, the citation relations between articles (Vu et al. 2011; Wang and Li 2013) may provide very useful information. However, incorporating relational information into deep neural network (DNN) models like SDAE is non-trivial since with the relational data, the samples are no longer i.i.d., which is the assumption underlying DNN models.

In this paper, we propose novel methods to address the above challenges. The main contributions of this paper are summarized as follows:

- We adapt SDAE and use it in conjunction with PMF (or a simplified version of CTR) to significantly boost the recommendation performance.
- To satisfy the need for relational deep learning, we develop a probabilistic formulation for SDAE and, by extending this probabilistic SDAE, we propose a relational probabilistic model called relational SDAE (RSDAE) to integrate deep representation learning and relational learning in a principled way. Besides, RSDAE can be naturally extended to handle multi-relational data (with more details provided in the supplementary material).
- Extensive experiments on datasets from different domains show that our models outperform the state of the art.

Problem Statement and Notation

Assume we have a set of items (articles or movies) \( \mathbf{X}_c \) to be tagged, with \( \mathbf{X}^T_{c,j,s} \in \mathbb{R}^D \) denoting the content (attributes) of item \( j \). In the case of tagging articles (papers) in CiteULike, the items are papers, and the content information can be the bag-of-words representation of paper abstracts. Assume we have a set of \( I \) tags \( \{t_1, t_2, \ldots, t_I\} \) as candidates to be recommended to tag each item. Then a tag-item matrix \( \mathbf{R} \) can be used to represent the tagging information for all the items. Each matrix entry \( R_{ij} \) is a binary variable, where \( R_{ij} = 1 \) means that tag \( t_i \) is associated with item \( j \) and \( R_{ij} = 0 \) otherwise. Tag recommendation is to predict the missing values in \( \mathbf{R}_{c,j,s} = [R_{1,j}, R_{2,j}, \ldots, R_{I,j}]^T \) (i.e., recommend tags to items). Besides, we use \( \mathbf{I}_K \) to denote a \( K \)-dimensional identity matrix and \( \mathbf{S} = [s_1, s_2, \ldots, s_J] \) to denote the relational latent matrix with \( s_j \) representing the relational properties of item \( j \). Note that although we focus on tag recommendation for articles and movies in this paper, our proposed models are flexible enough to be used for other applications such as image and video tagging.

From the perspective of SDAE, the \( J \)-by-\( B \) matrix \( \mathbf{X}_c \) represents the clean input to the SDAE and the noise-corrupted matrix of the same size is denoted by \( \mathbf{X}_0 \). Besides, we denote the output of layer \( l \) of the SDAE, a \( J \)-by-\( K_l \) matrix, by \( \mathbf{X}_l \). Row \( j \) of \( \mathbf{X}_l \) is denoted by \( \mathbf{X}_{l,j,s} \). \( \mathbf{W}_l \) and \( \mathbf{b}_l \) are the weight matrix and bias vector of layer \( l \), \( \mathbf{W}_{l,n} \) denotes column \( n \) of \( \mathbf{W}_l \), and \( L \) is the number of layers. As a shorthand, we refer to the collection of all layers of weight matrices and biases as \( \mathbf{W}^+ \). Note that in our models an \( L/2 \)-layer SDAE corresponds to an \( L \)-layer network.

Probabilistic Stacked Denoising Autoencoders

In this section we will first have a brief review on SDAE and then give a probabilistic formulation of generalized SDAE, which will be a building block of our relational stacked denoising autoencoder (RSDAE) model.

Stacked Denoising Autoencoders

SDAE (Vincent et al. 2010) is essentially a feedforward neural network for learning representations of the input data by learning to predict the clean input itself in the output. Normally the hidden layer in the middle is constrained to be a narrow bottleneck and the input layer \( \mathbf{X}_0 \) is a noise-corrupted version of the clean input data. Learning of an SDAE involves solving the following regularized optimization problem:

\[
\min_{(\mathbf{W}_l,\mathbf{b}_l)} \| \mathbf{X}_c - \mathbf{X}_L \|^2_F + \lambda \sum_l (\| \mathbf{W}_l \|^2_F + \| \mathbf{b}_l \|^2_F),
\]

where \( \lambda \) is a regularization hyperparameter and \( \| \cdot \|_F \) denotes the Frobenius norm.

Probabilistic Stacked Denoising Autoencoders

If we treat both the clean input (bag-of-words) \( \mathbf{X}_c \) and the corrupted input \( \mathbf{X}_0 \) as observed variables, the generative process for the generalized probabilistic SDAE is as follows:

1. For each layer \( l \) of the SDAE network,
   - (a) For each column \( n \) of the weight matrix \( \mathbf{W}_l \), draw \( \mathbf{W}_{l,n} \sim \mathcal{N}(0, \lambda_w^{-1}\mathbf{I}_{K_l}) \).
   - (b) Draw the bias vector \( \mathbf{b}_l \sim \mathcal{N}(0, \lambda_w^{-1}\mathbf{I}_{K_l}) \).
   - (c) For each row \( j \) of \( \mathbf{X}_l \), draw \( \mathbf{X}_{l,j,s} \sim \mathcal{N}(\sigma(\mathbf{X}_{l-1,j,s} \mathbf{W}_l + \mathbf{b}_l), \lambda_s^{-1}\mathbf{I}_{K_l}) \).
2. For each item \( j \), draw a clean input \( \mathbf{X}_{c,j,s} \sim \mathcal{N}(\mathbf{X}_{l,j,s}, \lambda_n^{-1}\mathbf{I}_{B_j}) \).

3Note that while generation of the clean input \( \mathbf{X}_c \) from \( \mathbf{X}_L \) is part of the generative process of the probabilistic SDAE, generation of the noise-corrupted input \( \mathbf{X}_0 \) from \( \mathbf{X}_c \) is an artificial noise injection process to help the SDAE learn a more robust feature representation.
Relational Stacked Denoising Autoencoders

Model Formulation

We formulate RSDAE as a novel probabilistic model which can seamlessly integrate layered representation learning and the relational information available. This way our model can learn simultaneously the feature representation from the content information and the relation between items. The graphical model of RSDAE is shown in Figure 1 and the generative process is listed as follows:

1. Draw the relational latent matrix $S$ from a matrix variate normal distribution (Gupta and Nagar 2000):

$$S \sim \mathcal{N}_{K,J}(0, I_K \otimes (\lambda_s L_a)^{-1}).$$ (1)

2. For layer $l$ of the SDAE where $l = 1, 2, \ldots, \frac{L}{2} - 1$,

(a) For each column $n$ of the weight matrix $W_l$, draw $W_{l,n} \sim \mathcal{N}(0, \lambda_w^{-1} I_{K_l})$.

(b) Draw the bias vector $b_l \sim \mathcal{N}(0, \lambda_w^{-1} I_{K_l})$.

(c) For each row $j$ of $X_l$, draw $X_{l,j} \sim \mathcal{N}(\sigma(X_{l-1,j} W_l + b_l), \lambda_s^{-1} I_{K_l})$.

3. For layer $\frac{L}{2}$ of the SDAE network, draw the representation vector for item $j$ from the product of two Gaussians (PoG) (Gales and Airey 2006):

$$X_{\frac{L}{2},j} \sim \text{PoG}(\sigma(X_{\frac{L}{2}-1,j} W_l + b_l), s_j^T, \lambda_s^{-1} I_{K_l}, \lambda_r^{-1} I_{K_l}).$$

4. For layer $l$ of the SDAE network where $l = \frac{L}{2} + 1, \frac{L}{2} + 2, \ldots, L$,

(a) For each column $n$ of the weight matrix $W_l$, draw $W_{l,n} \sim \mathcal{N}(0, \lambda_w^{-1} I_{K_l})$.

(b) Draw the bias vector $b_l \sim \mathcal{N}(0, \lambda_w^{-1} I_{K_l})$.

(c) For each row $j$ of $X_l$, draw $X_{l,j} \sim \mathcal{N}(\sigma(X_{l-1,j} W_l + b_l), \lambda_s^{-1} I_{K_l})$.

5. For each item $j$, draw a clean input $X_{c,j} \sim \mathcal{N}(X_{\frac{L}{2},j}, \lambda_n^{-1} I_{B_l})$.

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Note that as the hyperparameter $\lambda_s$ approaches infinity, the last term will disappear and the model will degenerate to the original SDAE where $X_{l,j} = \sigma(X_{l-1,j} W_l + b_l)$. That is why we call it generalized SDAE.

Figure 1: Graphical model of RSDAE for $L = 4$. $\lambda_n$ is not shown here to prevent clutter.

Here, $\lambda_w$, $\lambda_s$, and $\lambda_n$ are hyperparameters and $\sigma(\cdot)$ is the sigmoid function.

Following the generative process above, maximizing the posterior probability is equivalent to maximizing the joint log-likelihood of $\{X_l\}$, $X_c$, $\{W_l\}$, and $\{b_l\}$ given $\lambda_s$, $\lambda_w$, and $\lambda_n$:

$$
\mathcal{L} = -\frac{\lambda_w}{2} \sum_l (\|W_l\|_F^2 + \|b_l\|_2^2) \\
- \frac{\lambda_s}{2} \sum_j \|X_{L,j} - X_{c,j}\|_2^2 \\
- \frac{\lambda_n}{2} \sum_j \|X_{L,j} - X_{c,j}\|_2^2 + \log p(S) - \frac{\lambda_r}{2} \sum_{j,j'} (s_j^T - X_{\frac{L}{2},j}) (s_{j'}^T - X_{\frac{L}{2},j'})
$$

Note that the hyperparameter $\lambda_s$ approaches infinity, the last term will disappear and the model will degenerate to the original SDAE where $X_{l,j} = \sigma(X_{l-1,j} W_l + b_l)$. That is why we call it generalized SDAE.

This theorem shows that the representation $X_{\frac{L}{2},j}$ can be represented as a PoG distribution:

$$X_{\frac{L}{2},j} \sim \text{PoG}(\sigma(X_{\frac{L}{2}-1,j} W_l + b_l), s_j^T, \lambda_s^{-1} I_{K_l}, \lambda_r^{-1} I_{K_l}).$$

In the SDAE network, the posterior probability is equivalent to maximizing the joint log-likelihood of $\{X_l\}$, $X_c$, $\{W_l\}$, and $\{b_l\}$ given $\lambda_s$, $\lambda_w$, $\lambda_l$, $\lambda_r$, and $\lambda_n$:

$$
\mathcal{L} = -\frac{\lambda_l}{2} \text{tr}(S S^T) - \frac{\lambda_r}{2} \sum_j \|s_j^T - X_{\frac{L}{2},j}\|_2^2 \\
- \frac{\lambda_s}{2} \sum_j \|X_{L,j} - X_{c,j}\|_2^2 \\
- \frac{\lambda_n}{2} \sum_j \|X_{L,j} - X_{c,j}\|_2^2 + \log p(S) - \frac{\lambda_r}{2} \sum_{j,j'} (s_j^T - X_{\frac{L}{2},j}) (s_{j'}^T - X_{\frac{L}{2},j'})
$$
where \( X_{i,j,s} = \sigma(X_{i-1,j,s}W_l + b_l) \). Similar to the
generalized SDAE, taking \( \lambda_s \) to infinity, the last term of
the joint log-likelihood will vanish. Note that the first term
\(-\frac{1}{2t}\text{tr}(S^{-1}S^T)\) corresponds to \( \log p(S) \) in the matrix
variate distribution in Equation (2). Besides, by simple
manipulation (details can be found in the supplementary
material), we have \( \text{tr}(S^{-1}S^T) = \sum_{k=1}^{K} S_{k,s}^T S_{k,s} \), where
\( S_{k,s} \) denotes the kth row of \( S \). As we can see, maximizing
\(-\frac{1}{2t}\text{tr}(S^T S)\) is equivalent to making \( s_k \) closer to \( s_j \) if
item \( j \) and item \( j' \) are linked (namely \( A_{j,j'} = 1 \)).

Learning Relational Representation

We now derive an EM-style algorithm for maximum a
posteriori (MAP) estimation.

In terms of the relational latent matrix \( S \), we first fix all
rows of \( S \) except the kth one \( S_{k,s} \), and then update \( S_{k,s} \).
Specifically, we take the gradient of \( \mathcal{L} \) with respect to \( S_{k,s} \),
set it to 0, and get the following linear system:

\[
(\lambda_t S_a + \lambda_r I) S_{k,s} = \lambda_r X_T^{I,ik}.
\]

A naive approach is to solve the linear system by setting
\( S_{k,s} = (\lambda_t S_a + \lambda_r I)^{-1} X_T^{I,ik} \). Unfortunately, the
complexity is \( O(J^3) \) for a single update. Similar to (Li
and Yeung 2009), the steepest descent method (Shewchuk
1994) is used to iteratively update \( S_{k,s} \):

\[
S_{k,s}(t + 1) \leftarrow S_{k,s}(t) + \delta(t)r(t)
\]

\[
\delta(t) \leftarrow \frac{\lambda_r X_T^{I,ik} - (\lambda_t S_a + \lambda_r I)S_{k,s}(t)}{r(t)^T r(t)}
\]

As discussed in (Li and Yeung 2009), the use of steepest
descent method dramatically reduces the computation cost
each iteration from \( O(J^3) \) to \( O(J) \).

Given \( S \), we can learn \( W_l \) and \( b_l \) for each layer using the
back-propagation algorithm. By alternating the update of \( S \),
\( W_l \), and \( b_l \), a local optimum for \( \mathcal{L} \) can be found. Also,
techniques such as including a momentum term may help to
avoid being trapped in a local optimum.

Tag Recommendation

After the representation for each item is learned, we can
use a simplified version of CTR (Wang and Blei 2011) to
learn the latent vectors \( u_i \) for tag \( i \) and \( v_j \) for item \( j \).
Similar to (Wang and Blei 2011), predicted ratings \( R_{ij} \)
can be computed as the inner product of \( u_i \) and \( v_j \). Essentially
we will be maximizing the following objective function:

\[
\mathcal{L} = \frac{\lambda_u}{2} \sum_i \| u_i \|^2 + \frac{\lambda_v}{2} \sum_j \| v_j - X_{I,ik,s}^T \|^2
\]

\[
- \sum_{i,j} c_{ij} (R_{ij} - u_i^T v_j)^2
\]

where \( \lambda_u \) and \( \lambda_v \) are hyperparameters. \( c_{ij} \) is set to 1 for the
existing ratings and 0.01 for the missing entries.

Experiments

Datasets

For our experiments, we use three real-world datasets with
two (Wang and Blei 2011; Wang, Chen, and Li 2013) from
citeULike\(^4\) and one from MovieLens\(^5\). There are 7386 tags,
16980 articles (items), and 204987 tag-item pairs in the
first dataset, citeulike-a. For the second one, citeulike-t,
the numbers are 8311, 25975, and 134860. The third
dataset, movielens-plot, originally from MovieLens-10M
and enriched by us, contains 2988 tags, 7261 movies (items),
and 51301 tag-item pairs.

The text information (item content) extracted from the
titles and abstracts of the articles and from the plots of
movies has been preprocessed using the same procedure as
that in (Wang and Blei 2011). The sizes of the vocabulary are
8000, 20000, and 20000 for the three datasets respectively.

Regarding the relational information, we use the citation
networks for citeulike-a and citeulike-t. For movielens-plot
we have two types of relational information (two graphs):
co-staff graph and co-genre graph. Existence of an edge
in the co-staff graph means that the two connected movies
share more than one staff member and an edge in the
core-genre graph means that the two movies have identical
genre combination. The numbers of edges in the citation
networks are 44709 and 32665 for citeulike-a and citeulike-t,
respectively. For the co-staff graph in movielens-plot there
are 118126 edges in total and that number is 425495 for
the co-genre graph. Note that our RSDAE model can
support multi-relational data (like movielens-plot), though
we present the uni-relational setting in the previous section
for simplicity. Details of the full multi-relational SDAE can
be found in the supplementary material.

Evaluation Scheme

In each dataset, similar to (Wang, Chen, and Li 2013), \( P \)
items associated with each tag are randomly selected to form
the training set and all the rest of the dataset is used as the
test set. \( P \) is set to 1 and 10, respectively, to evaluate and
compare the models under both sparse and dense settings
in the experiments. For each value of \( P \), the evaluation is
repeated five times with different randomly selected training
sets and the average performance is reported.

Following (Wang and Blei 2011; Purushotham, Liu, and
Kuo 2012; Wang, Chen, and Li 2013), we use recall as the
performance measure since the rating information appears
in the form of implicit feedback (Hu, Koren, and Volinsky
2008; Rendle et al. 2009), which means a zero entry may
be due to irrelevance between the tag and the item or the
user’s ignorance of the tags when tagging items. As such,
precision is not suitable as a performance measure. Like
most recommender systems, we sort the predicted ratings
of the candidate tags and recommend the top \( M \) tags to the
target item. The recall@\( M \) for each item is defined as:

\[
\text{recall@}M = \frac{\text{number of tags the item is associated with in top } M}{\text{total number of tags the item is associated with}}
\]

\(^4\)CiteULike allows users to create their own collections
of articles. There are abstract, title, and tags for each article.
\(^5\)http://www.grouplens.org/datasets
The final reported result is the average recall over all items.

**Experimental Settings**

Experiments in (Wang, Chen, and Li 2013) have demonstrated that CTR and CTR-SR clearly outperform state-of-the-art content-based methods, co-occurrence based methods, and other hybrid methods. Due to space constraints, in the experiments we use only CTR (Wang and Blei 2011) and CTR-SR (Wang, Chen, and Li 2013) as baselines. CTR is a model combining LDA and PMF for recommendation. CTR-SR is a powerful extension of CTR in a sense that it seamlessly incorporates relational data into the model. We fix $K = 50$ and use a validation set to find the optimal hyperparameters for CTR and CTR-SR. For SDAE and RSDAE, tag recommendation can be divided into two steps: learning relational representation and PMF. We set $\lambda_r$ to infinity for efficient computation and fair comparison with SDAE. Furthermore, since there are only four terms left in Equation (3) after the last term vanishes, we can directly fix $\lambda_r = 1$. The remaining hyperparameters of the first step ($\lambda_l, \lambda_w,$ and $\lambda_h$) are found by grid search ($\lambda_w$ is the hyperparameter for weight decay and can be ignored if we choose not to use it) and hyperparameters of the second step are fixed to values the same as those of CTR. For the grid search, we split the training data and 5-fold cross validation is used.

On the SDAE side, a masking noise with a noise level of 0.3 is added to the clean input $X_0$ to obtain the corrupted input $X_c$. We use a fixed dropout rate of 0.1 (Hinton et al. 2012; Wager, Wang, and Liang 2013) to achieve adaptive regularization. For the network architecture, we set the number of non-bottleneck hidden units $K_l$ to 200. $K_0$ and $K_L$ are set to $B$, the number of words in the dictionary. $K_{L/2}$ is equal to $K$, the number of latent factors in PMF. For example, a 2-layer SDAE has an architecture of ‘20000-200-50-200-20000′ for the dataset movielens-plot.

**Performance Evaluation**

Figures 2, 3, and 4 show the recall@$M$ for all three datasets in the sparse and dense settings, with $M$ ranging from 50 to 300. As we can see, CTR-SR outperforms CTR by incorporating relational data into the model. What is surprising is that even without using any relational information, SDAE in conjunction with PMF still outperforms CTR-SR which utilizes abundant relational information, especially for citeulike-t as shown in Figure 3. Furthermore, RSDAE can achieve even higher recall by jointly performing representation learning and relational learning in a principled way.

Figure 5(left) shows the recall@$M$ of RSDAE for citeulike-t in the sparse setting when $L = 2, 4, 6$ (corresponding to 1-layer, 2-layer, and 3-layer RSDAE, respectively). As we can see, the recall increases with the number of layers. Similar phenomena can be observed for other datasets which are omitted here due to space constraints. Note that the standard deviations are negligible in all experiments (from $4.56 \times 10^{-5}$ to $3.57 \times 10^{-5}$). To prevent clutter, the standard deviations are not separately reported for all figures in this paper.

**Sensitivity to Hyperparameters**

Figure 5(right) shows how recall@$M$ is affected by the choice of hyperparameter $\lambda_n$ for movielens-plot in the sparse setting when $\lambda_r = 1$ and $\lambda_l = 100$. As shown in the figure, recall@$M$ increases with $\lambda_n$ initially and gradually decreases at some point after $\lambda_n = 1$. It is not very sensitive within a wide range of values, especially after the optimal point. Similar phenomena are observed for other hyperparameters like $\lambda_l$. More details can be found in the supplementary material.

**Case Study**

To gain a deeper insight into the difference between SDAE and RSDAE, we choose one example article from citeulike-a and one example movie from movielens-plot to conduct a case study. The experiments are conducted in the sparse setting for citeulike-a and in the dense setting
Table 1: Example items (one movie and one article) with recommended tags

<table>
<thead>
<tr>
<th>Example Article</th>
<th>Top topic 1: Mining the Peanut Gallery: Opinion Extraction and Semantic Classification of Product Reviews</th>
</tr>
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<tbody>
<tr>
<td>Top 10 recommended tags</td>
<td>SDAE</td>
</tr>
<tr>
<td>1. instance_within_labeled_concepts</td>
<td>no</td>
</tr>
<tr>
<td>2. consumer</td>
<td>yes</td>
</tr>
<tr>
<td>3. sentiment_analysis</td>
<td>no</td>
</tr>
<tr>
<td>4. summary</td>
<td>no</td>
</tr>
<tr>
<td>5. 31july09</td>
<td>no</td>
</tr>
<tr>
<td>6. medline</td>
<td>no</td>
</tr>
<tr>
<td>7. eit2</td>
<td>no</td>
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<tr>
<td>8. l2r</td>
<td>no</td>
</tr>
<tr>
<td>9. exploration</td>
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<tr>
<td>10. biomedical</td>
<td>no</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Example Movie</th>
<th>Top topic 1: E.T. the Extra-Terrestrial</th>
</tr>
</thead>
<tbody>
<tr>
<td>Top 10 recommended tags</td>
<td>SDAE</td>
</tr>
<tr>
<td>1. Saturn Award (Best Special Effects)</td>
<td>yes</td>
</tr>
<tr>
<td>2. Want</td>
<td>no</td>
</tr>
<tr>
<td>3. Saturn Award (Best Fantasy Film)</td>
<td>no</td>
</tr>
<tr>
<td>4. Saturn Award (Best Writing)</td>
<td>yes</td>
</tr>
<tr>
<td>5. Cool but freaky</td>
<td>no</td>
</tr>
<tr>
<td>6. Saturn Award (Best Director)</td>
<td>no</td>
</tr>
<tr>
<td>7. Oscar (Best Editing)</td>
<td>no</td>
</tr>
<tr>
<td>8. almost favorite</td>
<td>no</td>
</tr>
<tr>
<td>9. Steven Spielberg</td>
<td>yes</td>
</tr>
<tr>
<td>10. sequel better than original</td>
<td>no</td>
</tr>
</tbody>
</table>

for movielens-plot. We list the top 10 recommended tags provided by SDAE and RSDAE for the target items. Note that in the sparse setting recommendation is very challenging due to extreme sparsity of tagging information. As we can see in Table 1, the precisions for the target article are 10% and 60%, respectively. For the target movie the numbers are 30% and 60%. The huge gap shows that relational information plays a significant role in boosting the recommendation accuracy for the target items.

Looking into the recommended tag lists and the data more closely, we find that the example article ‘Mining the Peanut Gallery: Opinion Extraction and Semantic Classification of Product Reviews’ is a WWW paper about sentiment classification. As shown in the table, most of the recommended tags provided by SDAE are trivial or irrelevant while RSDAE can understand the focus of the article a lot better and achieve a precision up to 60%. Among the six tags correctly predicted by RSDAE, two of them are related to articles linked to the target article directly. This means RSDAE is not simply recommending tags associated to linked articles in the citation network. By jointly performing relational learning and deep representation learning, these two parts actually benefit from each other and yield additional performance gain.

A similar phenomenon is observed in the example movie ‘E.T. the Extra-Terrestrial’ directed by Steven Spielberg. RSDAE correctly recommends three more tags for the award-winning movie. Among the three, two tags are related to movies directly linked to the target one. Interestingly, although the remaining tag ‘Oscar (Best Music - Original Score)’ does not show up in the tag lists of the linked movies, we find that ‘E.T. the Extra-Terrestrial’ is directly linked to the movie ‘Raiders of the Lost Ark’ (also directed by Steven Spielberg), which was once nominated for Oscar’s academy award for best music. These results show that RSDAE as a relational representation learning model seems to do quite a good job in predicting award winners as well.

**Conclusion**

In this paper we first adapt SDAE to learn deep item representations for tag recommendation. Furthermore, we develop a probabilistic formulation for SDAE and, by extending this probabilistic SDAE, we propose RSDAE as a novel relational extension for integrating deep representation learning and relational learning in a principled way. Our model can also be naturally extended to handle multi-relational data due to its probabilistic nature. Experiments on real-world datasets from different domains show that our models are effective and outperform the state of the art. Besides, our framework is general enough to be adapted for other deep learning models like CNN as well.

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**References**


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